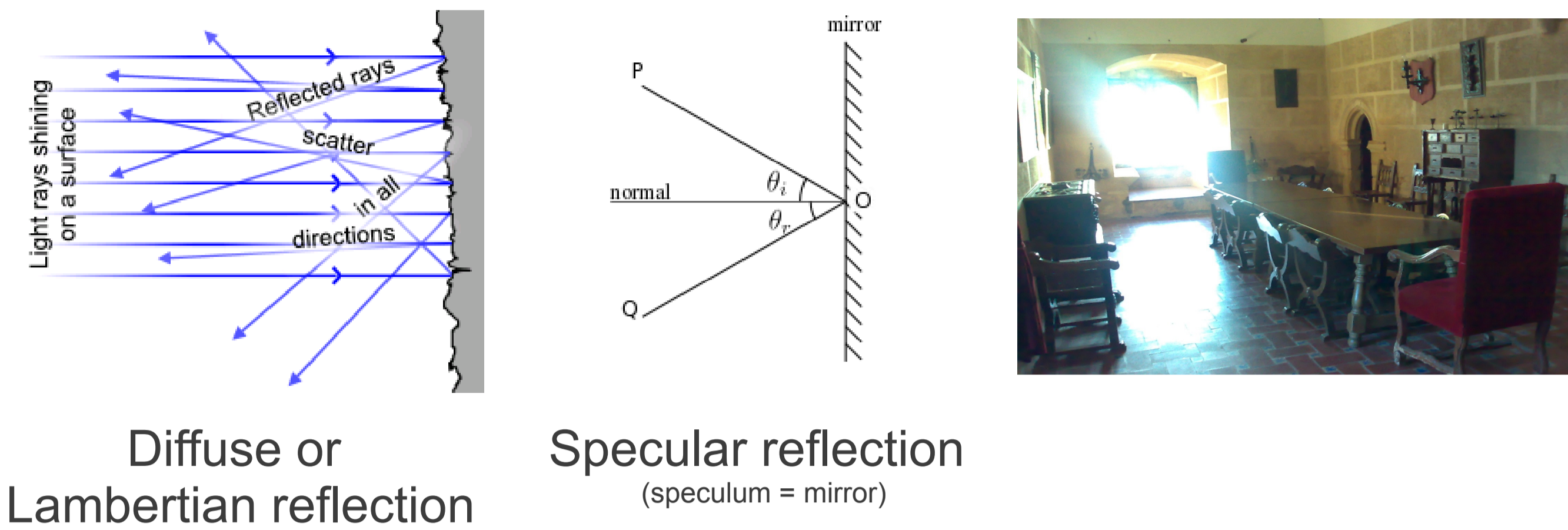


# A geometrical method of diffuse and specular image components separation

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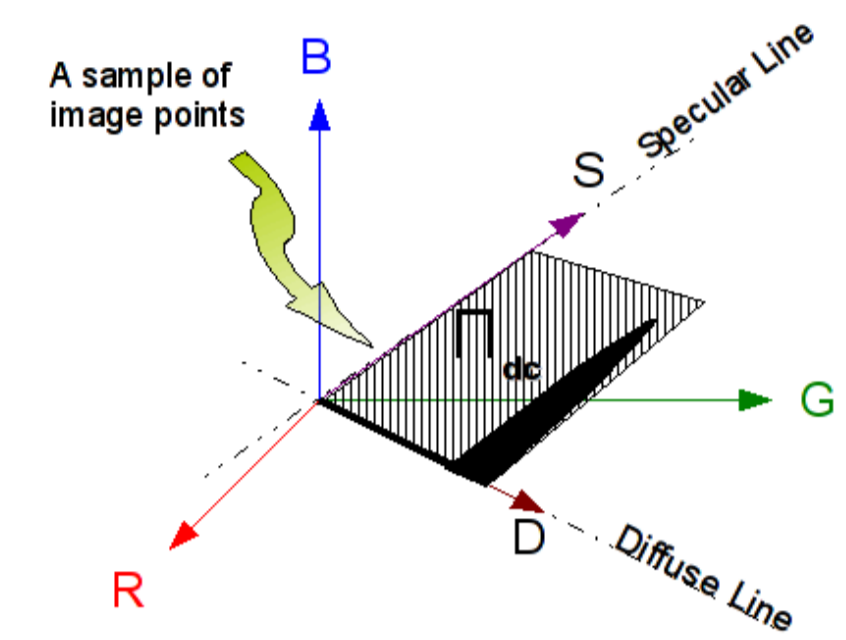
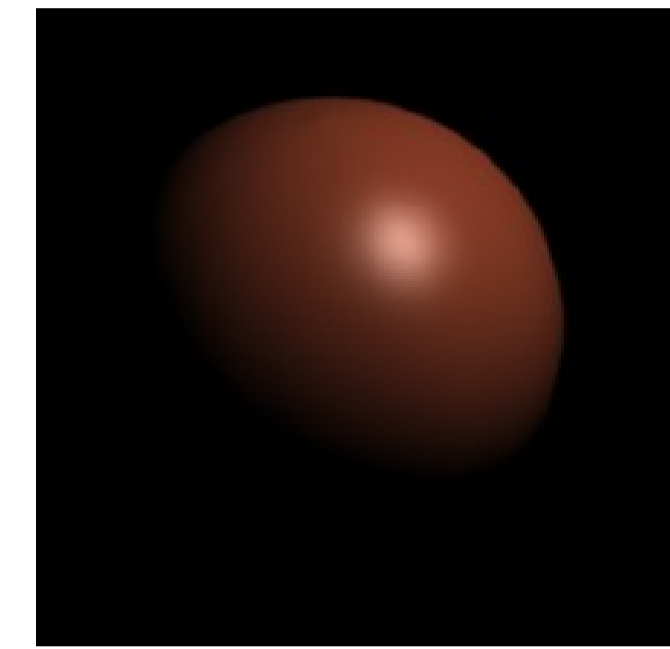
## Diffuse and specular Reflections



## Dichromatic Reflection Model

DRM explains the formation of the image of the observed surface as the addition of a diffuse component  $D$  and an specular component  $S$ .

Algebraically, the DRM is  $I(x) = md(x)D + ms(x)S$  where  $md$  and  $ms$  are the diffuse and specular component weights respectively.



## General Description of the Method

### 1. Chromatic line estimation:

Estimate the diffuse line  $L_d$  and the specular line  $L_s$

### 2. Dichromatization:

We compute the parameters of the chromatic plane in the RGB cube, and we project all the pixel colors into this plane. This step involves some additive noise removal.

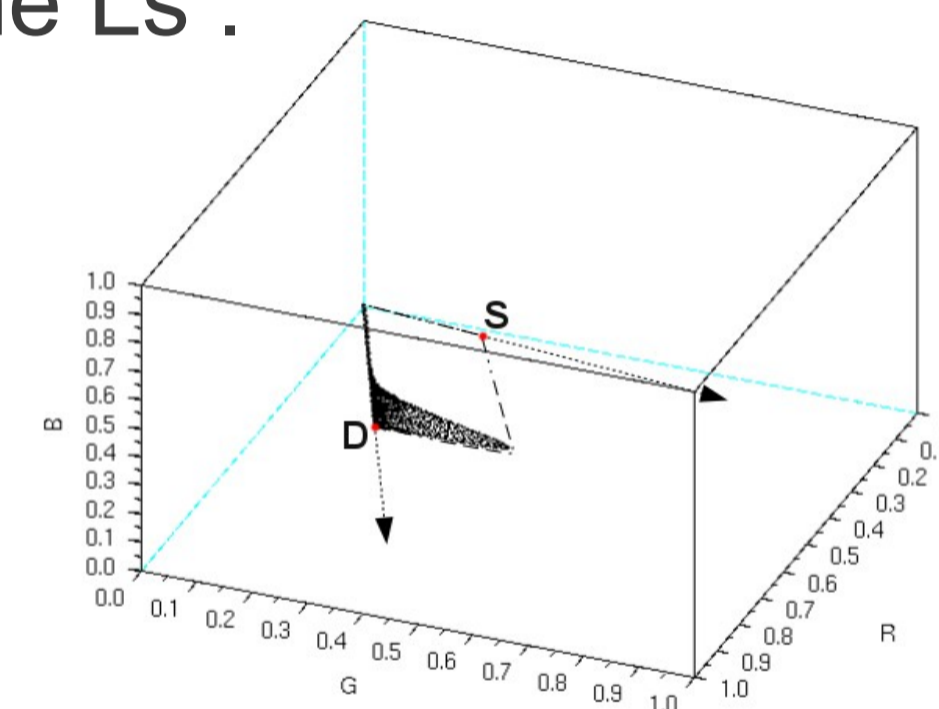
### 3. Component separation:

We compute the pure diffuse image component and the specular image component.

## Chromatic lines estimation

We can easily appreciate the two main directions in the data. The most clear is the one corresponding to the diffuse line  $L_d$  which rises from the coordinate system origin.

The second, less dened, appearing at the end of the diffuse elongation, is the specular direction identified by the specular line  $L_s$ .



We perform a Principal Component Analysis (PCA) which give us the direction of the chromatic line  
 Therefore the diffuse chromatic line is dened as

$$L_d : (r, g, b) = P + su ; \forall s \in \mathbb{R}$$

Analogously, we select the brightest pixels, obtaining a mean point  $Q$  in the RGB cube and the largest eigenvector for the specular color, therefore the specular chromaticity line is expressed as follows

$$L_s : (r, g, b) = Q + tv ; \forall t \in \mathbb{R}$$

## Dichromatization

Once we know the chromatic lines, we build the dichromatic plane  $\Pi$ , which is the best planar approximation to the color distribution in RGB. It can be expressed as follows:

$$\Pi : (r, g, b) = P + s\mathbf{u} + t\mathbf{v} ; \forall s, t \in \mathbb{R}, \text{ and the normal vector is } \mathbf{N} : \mathbf{u} \times \mathbf{v}, \text{ where } \times \text{ denotes the conventional vector product.}$$

To remove noise and regularize the image colors we project the pixel's colors into this dichromatic plane  $\Pi$ .

For each image point color in the RGB cube  $\mathbf{p}_i$  we compute the line  $L_{in} : (r, g, b) = \mathbf{p}_i + k\mathbf{N} ; \forall k \in \mathbb{R}$ , which is orthogonal to the dichromatic plane  $\Pi$ , and to regularize  $\mathbf{p}_i$  we compute its projection as the intersection of  $L_{in}$  with  $\Pi$ .

## Components Separation

Our goal is to bring the pixels to the chromatic line, that is  $\forall \mathbf{x} : ms(\mathbf{x}) = 0$ . We proceed as follows: for each regularized image point  $\mathbf{p}$  lying in the plane  $\Pi$  we draw the line

$$L_{is} : (r, g, b) = \mathbf{p} + t\mathbf{v} ; \forall t \in \mathbb{R}$$

where  $\mathbf{v}$  is the specular line vector director.

The pixel diffuse component corresponds to the intersection point  $\mathbf{pd}$  of this line with the diffuse line

$$L_d : (r, g, b) = P + su ; \forall s \in \mathbb{R}$$

and it exists because they lie in the same plane  $\Pi$  and they are not parallel lines.

## Components Separation

We have obtained  $I_d(\mathbf{x}) = md(\mathbf{x})D$  so that  $\forall \mathbf{x} : m(\mathbf{x}) = 0$ , and the resulting image  $I_d(\mathbf{x})$  is purely diffuse, without specular components.

Obtaining the specular image component is then trivial if we recall the DRM denition:

$$I_s(\mathbf{x}) = I(\mathbf{x}) - I_d(\mathbf{x}) = I(\mathbf{x}) - md(\mathbf{x})D = ms(\mathbf{x})S$$

## Some Experimental Results

