

# From dynamic classifier selection to dynamic ensemble selection Nikunj C. Oza, Kagan Tumer

#### **Eider Sánchez**







### Contenidos

- 1. Objective of the article
- 2. Introduction to classifier ensembles
- 3. Classifier ensemble methods
- 4. Real-World applications
- 5. Conclusions







### **Objective of the article**

- Introduce classifier ensembles
  - Definitions
    - Classifier ensembles
    - Bias/Variance tradeoff
    - Bayesian interpretation

#### □ Summarize leading ensemble methods

- Simple averaging
- Weighted averaging
- Stacking
- Bagging
- Boosting
- Order statistics

Show real-word applications, in 4 different domains:

- □ Remote sensing
- Person recognition
- □ One vs. all recognition
- Medicine







### **Classifier ensembles**

- Classification task:
  - Requires the construction of a statistical model that represents a mapping from input data to the appropriate outputs.
  - Model: intended to approximate the true mapping from the inputs to the outputs
  - □ Purpose: generate predictions of outputs for new, previously unseen inputs.
- Single classifier to make predictions for new examples.
  - □ BUT: many decisions affect the performance of that classifier.
  - □ Option A: selecting the best available classifier
    - BUT: distribution over new examples that the classifier may encounter during operation may vary
    - BUT: many classifiers are generally tried before a single classifier is selected. Therefore, valuable information discarded by ignoring the performance of all the other classifiers.
  - Option B: Classifier ensembles







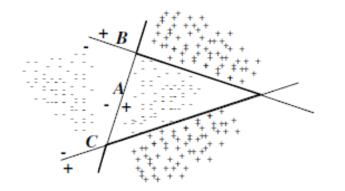
### **Classifier ensembles**

Classifier ensembles (combiners or committees)

\* Aggregations of several classifiers whose individual predictions are combined in some manner (e.g., averaging or voting) to form a final prediction.

Use all the available classifier information

□ Generally provide better and/or more robust solutions in most applications



#### Example:

An ensemble of linear classifiers (boldface line). Each line A, B, and C is a linear classifier.







# **Classifier ensemble methods**

- Simple averaging
- Weighted averaging
- Stacking
- ★ Bagging
- ✤ Boosting
- Order statistics







### **Classifier ensemble methods - Simple averaging**

If *M* classifiers  $(h_i^m(x), m$ 

 $\in \{1, 2, ..., M\}$ ) are available, the class  $C_i$  output of the averaging combiner is:

$$h_i^{\text{ave}}(x) = \frac{1}{N} \sum_{m=1}^M h_i^m(x)$$
(1)

### Benefits

□ Reduces the variance of the estimate of the output class posteriors

□ Simple: widely applied to real-world problems

□ Effective ensemble method, particularly in large complex data

- Problems
  - Reduces model error

$$E_{\text{model}}^{\text{ensemble}} = \frac{1 + \rho (M - 1)}{M} E_{\text{model}}$$

 $\rho$  : Average correlation among the errors of the different classifiers







## **Classifier ensemble methods - Weighted averaging**

Different classifier weight

$$h_i^{\text{ave}}(x) = \frac{1}{M} \sum_{m=1}^M w_m h_i^m(x)$$

- \* Added degrees of freedom  $\rightarrow$  better solutions
- But in practice
  - □ failed to provide improvement to justify its added complexity
  - When there is limited training data with which the weights can be properly estimated







## **Classifier ensemble methods - Stacking**

- ★ Actively seeks to improve the performance of the ensemble by correcting the errors
- Stacked generalization addresses the issue of classifier bias with respect to a training set, and aims at learning and using these biases to improve classification
- The main concept is to use a new classifier to correct the errors of a previous classifier







## **Classifier ensemble methods - Bagging**

- Bootstrapped Aggregating (Bagging)
  - Combines voting with a method for generating the classifiers that provide the votes
  - □ Allow each base classifier to be trained with a different random subset of the patterns with the goal of bringing about diversity in the base classifiers.
- improve upon their base models more if the base model learning algorithms are unstable (ej. Decision trees)
  - □ differences in their training sets tend to induce significant differences in the models

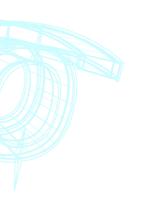






### **Classifier ensemble methods - Bagging**

Bootstrapped Aggregating (Bagging)



Bagging(T,M)For each m = 1, 2, ..., M,  $T_m = Sample\_With\_Replacement(T, |T|)$   $h_m = L_b(T_m)$ Return  $h_{fin}(x) = \operatorname{argmax}_{y \in Y} \sum_{m=1}^M I(h_m(x) = y)$ 

```
\begin{split} \mathbf{Sample_With_Replacement}(T,N) \\ S &= \emptyset \\ \text{For } i &= 1, 2, \dots, N, \\ r &= random\_integer(1,N) \\ \text{Add } T[r] \text{ to } S. \\ \text{Return } S. \end{split}
```







### **Classifier ensemble methods - Boosting**

### AdaBoost algoritm

Generates a sequence of base models with different weight distributions over the training set

 $\begin{aligned} \mathbf{AdaBoost}(\{(x_1, y_1), \dots, (x_N, y_N)\}, L_b, M) \\ \text{Initialize } D_1(n) &= 1/N \text{ for all } n \in \{1, 2, \dots, N\}. \\ \text{For } m &= 1, 2, \dots, M: \\ h_m &= L_b(\{(x_1, y_1), \dots, (x_N, y_N)\}, D_m). \\ \text{Calculate the error of } h_m : \epsilon_m &= \sum_{n:h_m(x_n) \neq y_n} D_m(n). \\ \text{If } \epsilon_m &\geq 1/2 \text{ then,} \\ &\text{set } M = m-1 \text{ and abort this loop.} \\ \text{Update distribution } D_m: \end{aligned}$ 

$$D_{m+1}(n) = D_m(n) \times \begin{cases} \frac{1}{2(1-\epsilon_m)} & \text{if } h_m(x_n) = y_n \\ \frac{1}{2\epsilon_m} & \text{otherwise} \end{cases}$$

Output the final model:

 $h_{fin}(x) = \operatorname{argmax}_{y \in Y} \sum_{m:h_m(x)=y} \log \frac{1-\epsilon_m}{\epsilon_m}.$ 





### **Classifier ensemble methods – Order statistics**

- Order statistics combiners that selectively pick a classifier on a per sample basis
- Model error

 $E_{\text{model}}^{\text{ensemble}} = \alpha E_{\text{model}}$ 

□ Alpha is a factor that depends on the number of classifiers M and the order statistic chosen and the error model

Error reduction factors  $\alpha$ , for the min, max and med combiners (Gaussian Error Model)

| М  | OS combiners |       |
|----|--------------|-------|
|    | min/max      | med   |
| 1  | 1.000        | 1.000 |
| 2  | 0.682        | 0.532 |
| 3  | 0.560        | 0.449 |
| 4  | 0.492        | 0.305 |
| 5  | 0.448        | 0.287 |
| 10 | 0.344        | 0.139 |
| 15 | 0.301        | 0.102 |
| 20 | 0.276        | 0.074 |







## **Real-world applications**

- Remote sensing
- Person recognition
- ✤ One vs. all recognition
- Medicine







# **Real-world applications – Remote sensing**

- Classification algorithms needs
  - □ large number of inputs
    - patterns collected repeatedly for large spaces

#### □ large number of features

• data is collected across hundreds of bands

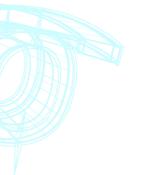
#### □ large number of outputs

 classes cover many types of terrain (forest, agricultural area, water) and manmade objects (houses, streets)

#### missing or corrupted data

- different bands or satellites may fail to collect data at certain times
- poorly labeled (or unlabeled) data
  - data needs to be post-processed and assigned to classes









# **Real-world applications – Remote sensing**

- Example applications
  - □ Random forests and mountainous terrain
  - □ Majority voting for agricultural land
  - Hierarchical classification of wetlands
  - □ Information fusion for Urban areas

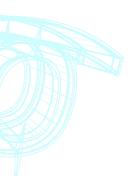






### **Real-world applications – Person recognition**

- Person recognition is the problem of verifying the identity of a person using characteristics of that person, typically for security applications
  - □ Iris recognition
  - □ fingerprint recognition
  - □ face recognition
  - behavior recognition
    - such as speech and handwriting
    - recognizing characteristics of a person, as opposed to depending upon specific knowledge that the person may have (such as usernames and passwords for computer account access)
- Problems
  - □ Involve multiple types of features
  - □ Difficulty in collecting good data
  - Different misclassification costs
    - Example, denying system access to a legitimate user vs. allowing access to an illegitimate user







## **Real-world applications – Person recognition**

- Example applications
  - □ Unobtrusive person identification
  - □ Face recognition
  - □ Multi-modal person recognition
  - □ User-specific speech recognition







## **Real-world applications – One vs. all recognition**

### Different types

#### Anomaly detection

- problem of detecting unusual patterns
- i.e. what does not fit into the set of identified patterns

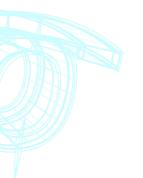
#### □ Target recognition

• finding what fits into an identified pattern

#### Intrusion detection

- solved both ways:
- A. target recognition: look for one of a set of known types of attacks
- B. anomaly detection : look for anomalies in the usage patterns



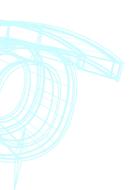






# **Real-world applications – One vs. all recognition**

- Example applications
  - □ Modular intrusion detection
  - □ Hierarchical intrusion detection
  - □ Intrusion detection in mobile ad-hoc networks









## **Real-world applications – Medicine**

- Different applications:
  - analyzing X-ray images, human genome analysis, and examining sets of medical test data to look for anomalies.
  - □ Root of all these problems: assessing the health of human beings

### Characteristics

limited training and test examples

• i.e., few training examples due to the nature of problem and privacy concerns

#### imbalanced datasets

• ie., very few anomalies or examples of patients with a disease

#### too many attributes

• i.e., often many more than the number of training and test examples

#### different misclassification costs

• i.e., false negatives significantly worse than false positives.

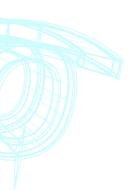






# **Real-world applications – Medicine**

- Example applications
  - Pharmaceutical molecule classification
  - □ MRI classification
  - □ ECG classification









### Conclusions

 Each ensemble method has different properties that make it better suited to particular types of classifiers and applications

- New applications, domains with complex and rich data
- Research areas:
  - □ Ensemble methods oriented at handling large amounts of diverse data
  - □ Clustering algorithms
  - □ Distributed classifier ensembles using active/agent-based methods











