

# 2-D Shape Representation and Recognition by Lattice Computing Techniques

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# The Problem:

Classify 2-D Shapes in 70 classes ...



(a) class “chicken”



(b) class “bird”

...from the MPEG-7 benchmark of binary images

In a data pre-processing step, for each 2-D shape, we extracted three populations of *Descriptors*\* including

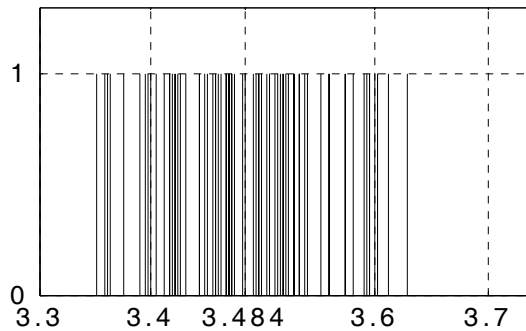
- $N_{FD} = 32$  Fourier Descriptors (FD),
- $N_{ART} = 112$  Angular Radial Transform (ART) Descriptors, and
- $N_{IM} = 6$  Image Moments (IM) Descriptors.

\*A *Descriptor* is a real number.

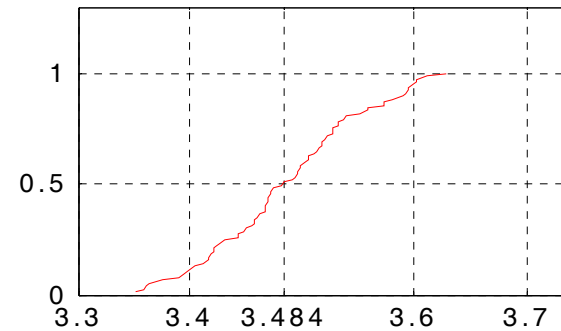
- A population of Descriptors was represented by an Intervals' Number (IN) as follows.

# IN representation of a Descriptors' population

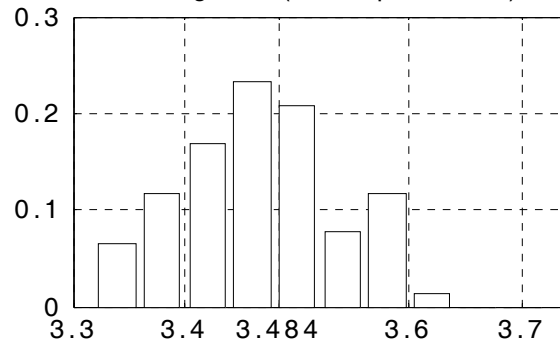
data samples



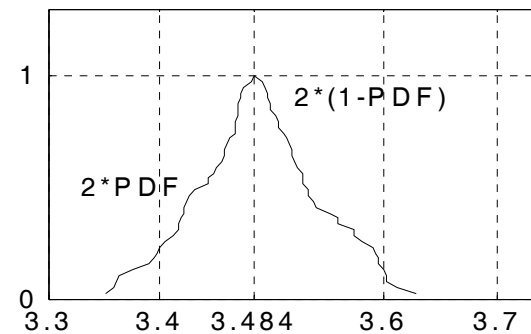
PDF: integral of the histogram



histogram (of frequencies)



corresponding IN

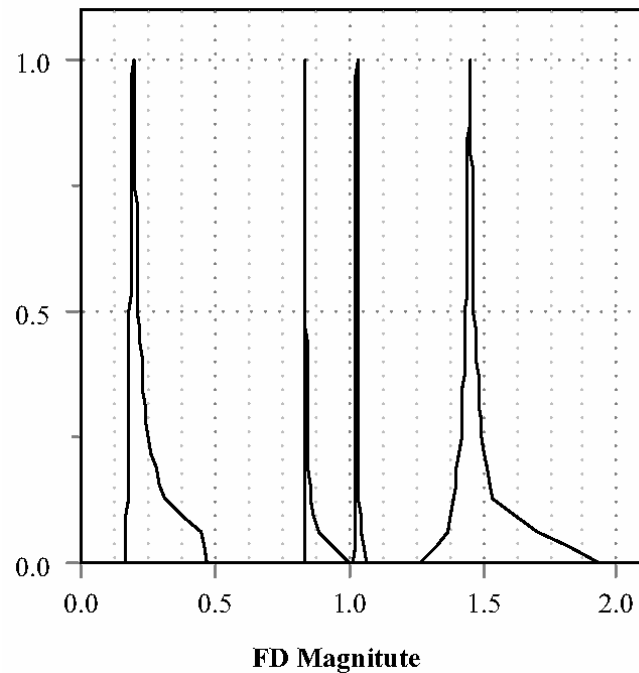


In conclusion,

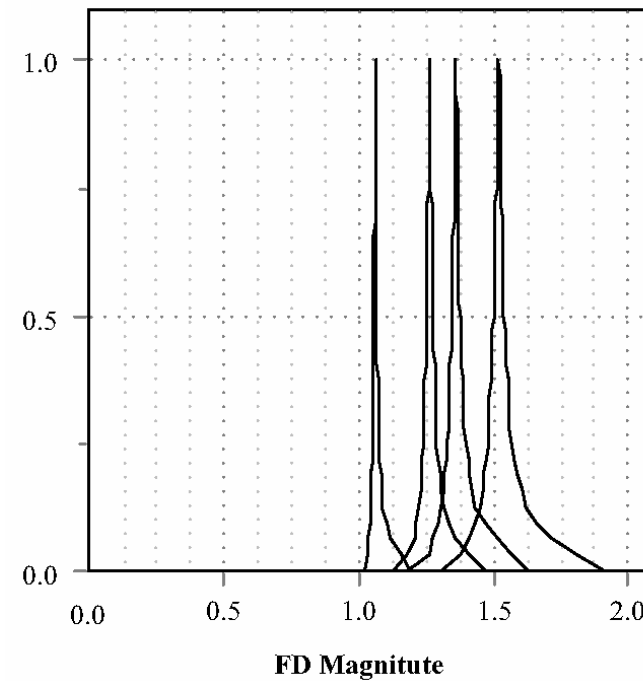
- a binary image was represented by three INs

Examples of INs induced from populations of Descriptors follow.

# INs induced from FD descriptors

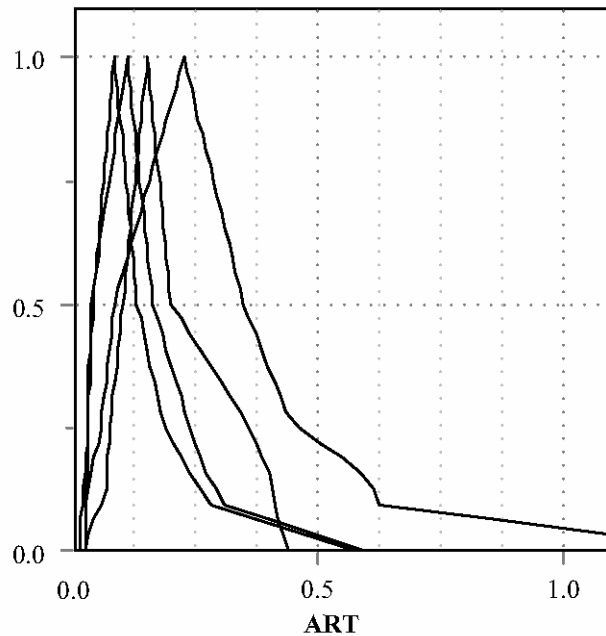


(a) INs for 4 "chicken"

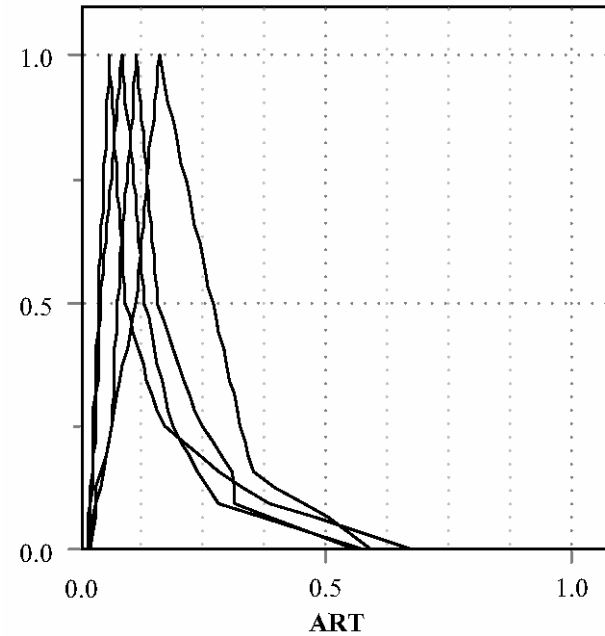


(b) INs for 4 "bird"

# INs induced from ART descriptors



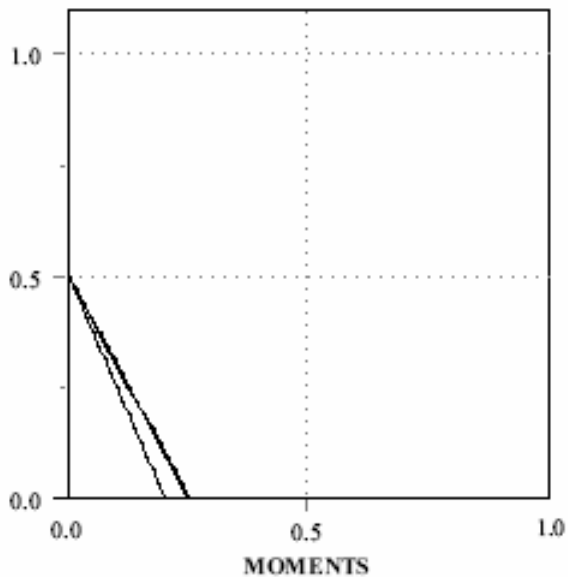
(a) INs for 4 "chicken"



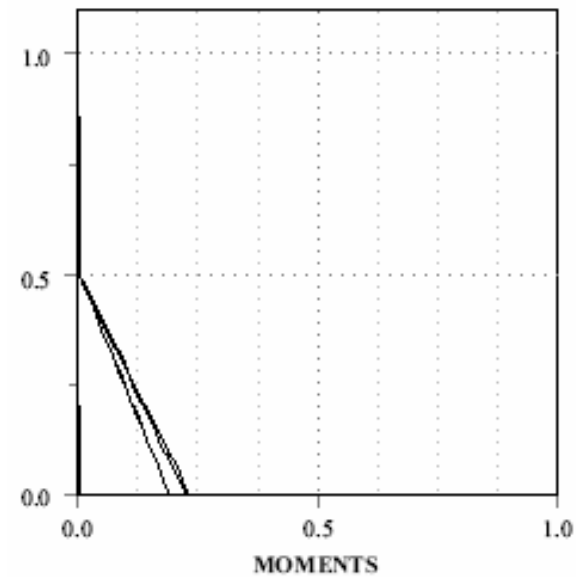
(b) INs for 4 "bird"



# INs induced from IM descriptors



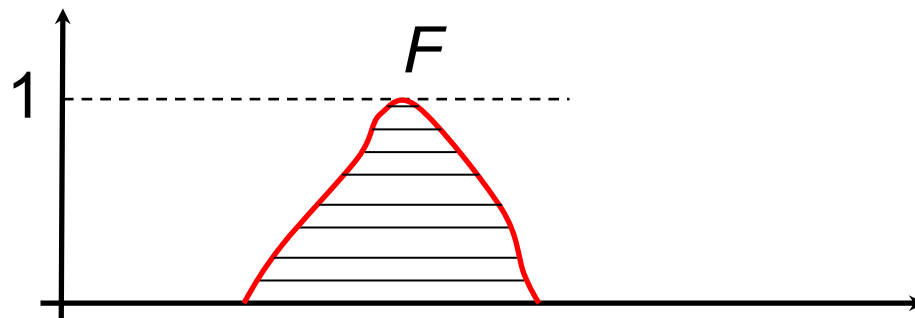
(a) INs for 4 "chicken"



(b) INs for 4 "bird"

# IN Representations & Mathematical Instruments

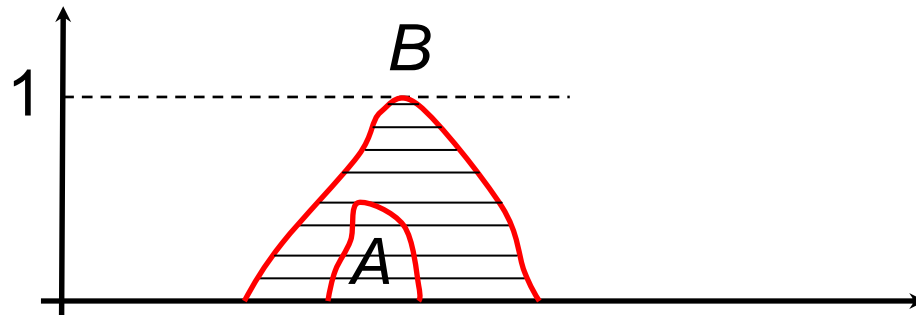
An Intervals' Number (IN)  $F$  can be represented, either by a *membership function* or, equivalently, by its (interval)  $\alpha$ -cuts.



Let  $F$  denote the space of INs. Then,

- $(F, \leq)$  is a complete lattice

# An interval-IN



- The space of interval-INs is a complete lattice.

An *inclusion measure* function  $\sigma: L \times L \rightarrow [0, 1]$ , in a complete lattice  $(L, \leq)$  with minimum element  $0$ , by definition, satisfies conditions

- 1)  $\sigma(x, 0) = 0, x \neq 0$ .
- 2)  $\sigma(x, x) = 1, \forall x \in L$ .
- 3)  $u \leq w \Rightarrow \sigma(x, u) \leq \sigma(x, w)$ .
- 4)  $x \wedge y < x \Rightarrow \sigma(x, y) < 1$ .

An *inclusion measure*  $\sigma: L \times L \rightarrow [0, 1]$  is given by

$$\text{either } \sigma_{\vee}(x, y) = \sigma_{\vee}(x \leq y) = \frac{v(y)}{v(x \vee y)}$$

$$\text{or } \sigma_{\wedge}(x, y) = \sigma_{\wedge}(x \leq y) = \frac{v(x \wedge y)}{v(x)}$$

for either  $L=F$  or  $L=(\text{lattice of interval-INs})$

# Cartesian Product Extensions

- Consider complete lattices  $(L_i, \leq)$  each equipped with an inclusion measure function  $\sigma_i$ ,  $i \in \{1, \dots, N\}$ . Let  $\mathbf{x} = (x_1, \dots, x_N), \mathbf{y} = (y_1, \dots, y_N) \in L = L_1 \times \dots \times L_N$ . Then, both functions

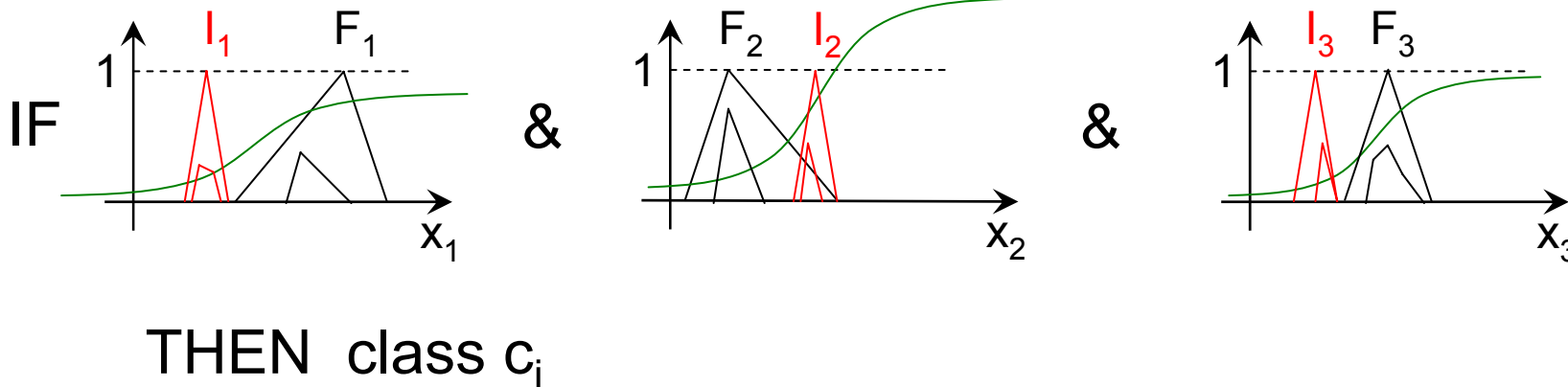
$$\sigma_{\wedge}(\mathbf{x} \leq \mathbf{y}) = \min_i \{\sigma_i(x_i \leq y_i)\} \quad \text{and}$$

$$\sigma_{\prod}(\mathbf{x} \leq \mathbf{y}) = \prod_i \sigma_i(x_i \leq y_i)$$

are inclusion measures.

# Rule-Based Decision-Making

- The degree of membership of a **red** interval-IN in class  $c_i$  equals  $\sigma((I_1, I_2, I_3) \leq (F_1, F_2, F_3))$ .





- The *size* of an interval  $[a_h, b_h]$  equals

$$S([a_h, b_h]) = v(b_h) - v(a_h),$$

- The *size* of a IN  $F = [a_h, b_h], h \in (0, 1]$  equals

$$S(F) = \int_0^1 S([a_h, b_h]) dh = \int_0^1 [v(b_h) - v(a_h)] dh$$

where function  $v: \mathbb{R} \rightarrow \mathbb{R}$  is strictly increasing.

## BIIN<sub>trn</sub>: Batch Interval-IN for training

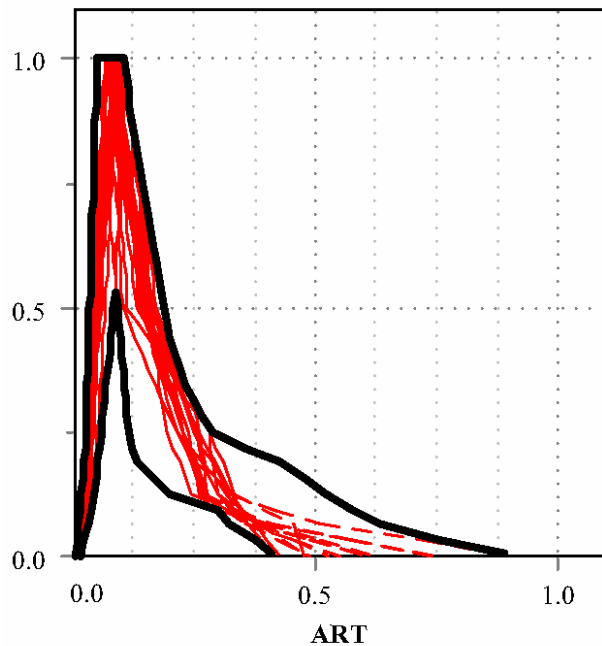
- Let  $(\delta_1, c(\delta_1)), \dots, (\delta_n, c(\delta_n))$  be labeled interval-INs for training.
- Consider a threshold  $S_\theta$ .
- Let  $(I, J) = \operatorname{argmin}\{S(\delta_i \vee \delta_j)\}: I \neq J \text{ and } c(\delta_i) = c(\delta_j)\}$ .
- **while**  $S(\delta_i \vee \delta_j) < S_\theta$  **do**
- Replace both  $\delta_i$  and  $\delta_j$  by  $\delta_i \vee \delta_j$ .
- Let  $(I, J) = \operatorname{argmin}\{S(\delta_i \vee \delta_j)\}: I \neq J \text{ and } c(\delta_i) = c(\delta_j)\}$ .
- **end while**

## BIIN<sub>tst</sub> : Batch Interval-IN for testing

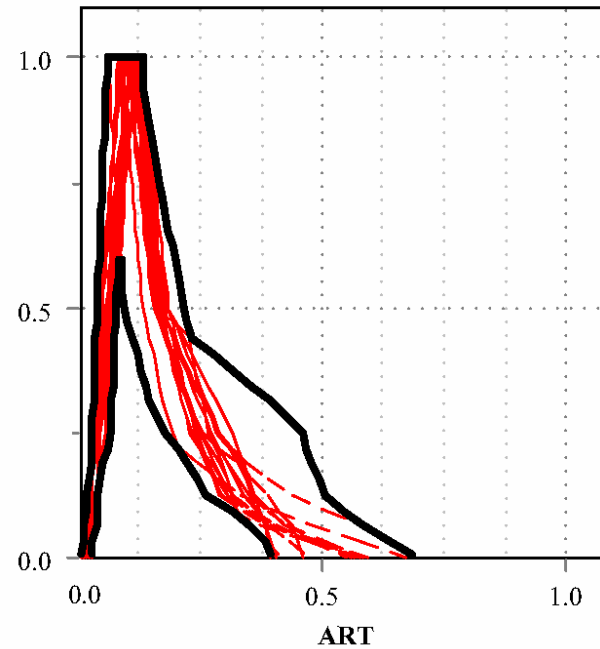
- Let  $(\delta_1, c(\delta_1)), \dots, (\delta_L, c(\delta_L))$  be labeled interval-INs.
- **For**  $i=1$  to  $n$  **do** //for each testing datum IN  $E_i$  do
- $J = \operatorname{argmax}\{\sigma[E_i, E_i] \leq \delta_\ell, \ell \in \{1, \dots, L\}\}.$
- Assign IN  $E_i$  to the class  $c(\delta_J)$ .
- **end for**

- Preliminary Experiments and Results

# Interval-INs computed from ART descriptors



(a) class "chicken"



(b) class "bird"

- Recognition rates > 90%
- Comparative experimental work is under way.